Name: Heights and Distances using Tables

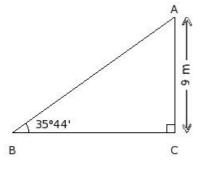
Chapter: Heights and Distances

Grade : ICSE Grade X

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A building stands vertically on the ground. From a point on the ground, the angle of elevation of the top of the building is found to be 35°44'. If the height of the building is 9 m, find the distance between the observation point and the top of the building.

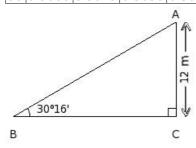
,					Fror	n Table	of Nat	tural Ta	angents	5						
1.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	35	0.7002	0.7028	0.7054	0.7080	0.7107	0.7133	0.7159	0.7186	0.7212	0.7239	4	9	13	17 2	22
					Fre	om Tab	le of N	atural 9	Sines							
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3' 4	ŀ' 5'	П
	35	0.5736	0.5750	0.5764	0.5779	0.5793	0.5807	0.5821	0.5835	0.5850	0.5864	2	5	7 9	9 12	2



(i) $18.41 \, \text{m}$ (ii) $10.41 \, \text{m}$ (iii) $20.41 \, \text{m}$ (iv) $12.41 \, \text{m}$ (v) $15.41 \, \text{m}$

A pole stands vertically on the ground. From a point on the ground, the angle of elevation of the top of the pole is found to be 30°16'. If the height of the pole is 12 m, find the distance between the observation point and the foot of the pole.

				Fror	m Table	of Nat	tural Ta	angents	5						
x° 0' 6' 12' 18' 24' 30' 36' 42' 48' 54' 1' 2' 3' 4' 5' 30 0.5774 0.5797 0.5820 0.5844 0.5867 0.5890 0.5914 0.5938 0.5961 0.5985 4 8 12 16 20															
30	0.5774	0.5797	0.5820	0.5844	0.5867	0.5890	0.5914	0.5938	0.5961	0.5985	4	8	12	16	20
				Fr	om Tab	le of N	atural	Sines							
χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
30	0.5000	0.5015	0.5030	0.5045	0.5060	0.5075	0.5090	0.5105	0.5120	0.5135	3	5	8	10 1	13

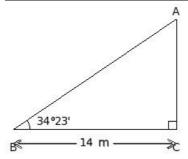


2.

(i) $25.56 \, \text{m}$ (ii) $15.56 \, \text{m}$ (iii) $20.56 \, \text{m}$ (iv) $17.56 \, \text{m}$ (v) $23.56 \, \text{m}$

A building stands vertically on the ground. From a point on the ground, the angle of elevation of the top of the building is found to be 34°23'. If the distance between the observation point and the foot of the building is 14 m, find the distance between the observation point and the top of the building.

				Froi	m Table	of Nat	tural Ta	angent	5						
χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
34	0.6745	0.6771	0.6796	0.6822	0.6847	0.6873	0.6899	0.6924	0.6930	0.6976	4	9	13	17	22
				Fror	m Table	of Nat	ural Co	sines							
χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	J 1	4' 5	1
3/1	0.8290	0.8281	0.8271	0.8261	0.8251	0.8241	0.8231	0.8221	0.8211	0.8202	2	3	5	7 8	3



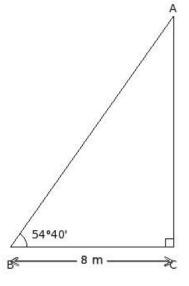
3.

4

(i) 16.96 m (ii) 19.96 m (iii) 11.96 m (iv) 13.96 m (v) 21.96 m

A building stands vertically on the ground. From a point on the ground, the angle of elevation of the top of the building is found to be 54°40′. If the distance between the observation point and the foot of the building is 8 m, find the height of the building.

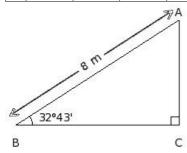
					Fro	m Table	e of Na	tural T	angent	S						
₽.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	54	1.3764	1.3814	1.3865	1.3916	1.3968	1.4019	1.4071	1.4124	1.4176	1.4229	9	17	26	34	13
					Froi	m Table	e of Na	tural C	osines							
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3' 4	5'	1
	54	0.5878	0.5864	0.5850	0.5835	0.5821	0.5807	0.5793	0.5779	0.5764	0.5750	2	5	7 9	12	1



(i) 6.28 m (ii) 16.28 m (iii) 8.28 m (iv) 14.28 m (v) 11.28 m

A pole stands vertically on the ground. From a point on the ground, the angle of elevation of the top of the pole is found to be 32°43'. If the distance between the observation point and the top of the pole is 8 m, find the height of the pole.

				Fr	om Tab	le of N	atural	Sines							
χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
32	0.5299	0.5314	0.5329	0.5344	0.5358	0.5373	0.5388	0.5402	0.5417	0.5432	2	5	7	10	12
				Fror	n Table	of Nat	ural Co	sines							
χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
32	0.8480	0.8471	0.8462	0.8453	0.8443	0.8434	0.8425	0.8415	0.8406	0.8393	2	3	5	6	8



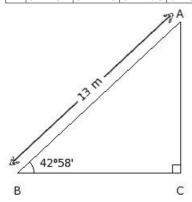
5.

6

(i) 2.32 m (ii) 4.32 m (iii) 5.32 m (iv) 3.32 m (v) 6.32 m

A tower stands vertically on the ground. From a point on the ground, the angle of elevation of the top of the tower is found to be 42°58'. If the distance between the observation point and the top of the tower is 13 m, find the distance between the observation point and the foot of the tower.

					Fre	om Tab	le of Na	atural S	Sines							
Э.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	42	0.6691	0.6704	0.6717	0.6730	0.6743	0.6756	0.6769	0.6782	0.6794	0.6807	2	4	6	9	11
					Froi	m Table	e of Na	tural Co	osines							
	х°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	42	0.7431	0.7420	0.7408	0.7396	0.7385	0.7373	0.7361	0.7349	0.7337	0.7325	2	4	6	8	10



(i) $8.51\,\mathrm{m}$ (ii) $9.51\,\mathrm{m}$ (iii) $11.51\,\mathrm{m}$ (iv) $10.51\,\mathrm{m}$ (v) $7.51\,\mathrm{m}$

The upper part of a tree is broken into two parts without being detatched. It makes an angle of 51°59' with the ground. The top of the tree touches the ground at a distance of 20 m from the foot of the tree . Find the height of the tree before it was broken.

_					Fro	m Tabl	e of Na	tural Ta	angent	S					
/.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1' 2'	3'	4'	5'
	51	1.2349	1.2393	1.2437	1.2484	1.2527	1.2572	1.2617	1.2662	1.2708	1.2753	8 15	23	30	38
					Fro	m Table	e of Na	tural Co	osines						
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1' 2'	3' 4	<u>' 5'</u>	7
										0.6184					_

(i) 42.42 m (ii) 44.42 m (iii) 50.42 m (iv) 47.42 m (v) 52.42 m

There are two temples one on each bank of a river, just opposite to each other. One of the temples is 110 m high. As observed from the top of this temple, the angles of depression of the top and foot of the other temple are $42^{\circ}6'$ and $50^{\circ}11'$ respectively. Find the width of the river .

_					Fro	m Table	e of Na	tural Ta	angent	5						
8.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	42	0.9004	0.9036	0.9067	0.9099	0.9131	0.9163	0.9195	0.9228	0.9260	0.9293	5	11	16	21	27
					Fro	m Table	e of Na	tural Ta	angent	5						
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	50	1.1918	1.1960	1.2002	1.2045	1.2088	1.2131	1.2174	1.2218	1.2261	1.2305	7	14	22	29	36

(i) 94.70 m (ii) 91.70 m (iii) 96.70 m (iv) 86.70 m (v) 88.70 m

There are two temples one on each bank of a river, just opposite to each other. One of the temples is 80 m high. As observed from the top of this temple, the angles of depression of the top and foot of the other temple are 40°44' and 51°21' respectively. Find the height of the other temple.

•		From Table of Natural Tangents x° 0' 6' 12' 18' 24' 30' 36' 42' 48' 54' 1' 2' 3' 4' 5' 40 0.8391 0.8421 0.8451 0.8481 0.8511 0.8541 0.8571 0.8601 0.8632 0.8662 5 10 15 20 25														
9.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4' 5	T
	40	0.8391	0.8421	0.8451	0.8481	0.8511	0.8541	0.8571	0.8601	0.8632	0.8662	5	10	15 2	20 2!	5
	From Table of Natural Tangents															
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4' 5	П
	51	1.2349	1.2393	1.2437	1.2484	1.2527	1.2572	1.2617	1.2662	1.2708	1.2753	8	15	23 3	30 38	8

(i) 21.92 m (ii) 27.92 m (iii) 19.92 m (iv) 24.92 m (v) 29.92 m

An observer 1.9 m tall, is 40 m away from a tower . The angle of elevation of the top of the tower from her eyes is $55^{\circ}44'$. Find the height of the tower .

10.					Fro	m Tabl	e of Na	tural Ta	angent	S						
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	55	1.4281	1.4335	1.4388	1.4442	1.4496	1.4550	1.4605	1.4659	1.4715	1.4770	9	18	27	36	45

(i) 57.61 m (ii) 60.61 m (iii) 63.61 m (iv) 55.61 m (v) 65.61 m

An aeroplane is flying horizontally 1700 m above the ground. From a point of observation, which lies exactly below the path of the aeroplane, the angle of elevation at a certain instant is 52° . After 40 sec , its elevation from the same point changes to 23° . Find the uniform speed of the aeroplane .

	From Table of Natural Tangents 1.														
11.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1' 2'	3'	4'	5'
	23	0.4245	0.4265	0.4286	0.4307	0.4327	0.4348	0.4369	0.4390	0.4411	0.4431	3 7	10	14 1	17
					Froi	m Table	e of Na	tural Ta	angent	S					
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1' 2	' 3'	4'	5'
	52	1.2799	1.2846	1.2892	1.2938	1.2985	1.3032	1.3079	1.3127	1.3175	1.3222	8 1	5 24	31	39

(i) 253.88 kmph (ii) 222.88 kmph (iii) 216.88 kmph (iv) 240.88 kmph

Two poles of equal height are standing opposite to each other on either side of a road which is 20 m wide. From a point between them on the road, the angles of elevation of the top of the poles are $27^{\circ}40'$ and $31^{\circ}33'$ respectively. Find the height of each pole and the distances of the point from the two poles .

					Fror	n Table	of Nat	tural Ta	ngents	5						
12.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	27	0.5095	0.5117	0.5139	0.5161	0.5184	0.5206	0.5228	0.5250	0.5272	0.5295	4	7	11	15	18
					Fror	n Table	of Nat	tural Ta	ngents	5						
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	31	0.6009	0.6032	0.6056	0.6080	0.6104	0.6128	0.6152	0.6176	0.6200	0.6224	4	8	12	16	20

- (i) height = 4.66 m, distances away = 8.21 m, 9.79 m (ii) height = 3.66 m, distances away = 7.21 m, 8.79 m
- (iii) height = 7.66 m, distances away = 11.21 m, 12.79 m
- (iv) height = 6.66 m, distances away = 10.21 m, 11.79 m
- (v) height = 5.66 m, distances away = 9.21 m, 10.79 m

From the top of a light house which is 45 m high from the sea level, the angles of depression of two ships are 42°59' and 33°53'. If one ship is exactly behind the other on the same side of the light house, find the distance between the two ships.

10		From Table of Natural Tangents													
13.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2' 3'	4'	5'
	42	0.9004	0.9036	0.9067	0.9099	0.9131	0.9163	0.9195	0.9228	0.9260	0.9293	5 1	11 16	21	27
		From Table of Natural Tangents													
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1' 2	2' 3'	4'	5'
	33	0.6494	0.6519	0.6544	0.6569	0.6594	0.6619	0.6644	0.6669	0.6694	0.6720	4	8 13	17	21

(i) 23.73 m (ii) 18.73 m (iii) 15.73 m (iv) 13.73 m (v) 21.73 m

From the top of a 15 m high building, the angle of elevation of the top of a cable tower is $46^{\circ}3'$ and the angle of depression of its foot is $43^{\circ}24'$. Find the height of the cable tower.

					Fro	m Tabl	e of Na	tural Ta	angent	S						
14.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	46	1.0355	1.0392	1.0428	1.0464	1.0501	1.0538	1.0575	1.0612	1.0649	1.0686	6	12	18	25	31
	From Table of Natural Tangents															
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	43	0.9325	0.9358	0.9391	0.9424	0.9457	0.9490	0.9523	0.9556	0.9590	0.9623	6	11	17	22	28

(i) 28.45 m (ii) 36.45 m (iii) 26.45 m (iv) 34.45 m (v) 31.45 m

The angle of elevation of the top of a building from the foot of a tower is 23°52'. The angle of elevation of the top of the tower from the foot of the building is 21°6'. If the height of the tower is 30 m, find the height of the building .

		From Table of Natural Tangents														
15.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	23	0.4245	0.4265	0.4286	0.4307	0.4327	0.4348	0.4369	0.4390	0.4411	0.4431	3	7	10	14	17
	From Table of Natural Tangents															
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	21	0.3839	0.3859	0.3879	0.3899	0.3919	0.3939	0.3959	0.3979	0.4000	0.4020	3	7	10	13	17

(i) 34.40 m (ii) 31.40 m (iii) 29.40 m (iv) 37.40 m (v) 39.40 m

A flag is hoisted at the top of a building . From a point on the ground, the angle of elevation of the top of the flag staff is 45°31' and the angle of elevation of the top of the building is 27°45'. If the height of the building is 7 m, find the height of the flag staff .

1.0		From Table of Natural Tangents														
16.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	27	0.5095	0.5117	0.5139	0.5161	0.5184	0.5206	0.5228	0.5250	0.5272	0.5295	4	7	11 :	15 1	18
					Fro	m Tabl	e of Na	tural Ta	angent	5						
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1'	2'	3'	4'	5'
	45	1.0000	1.0035	1.0070	1.0105	1.0141	1.0176	1.0212	1.0247	1.0283	1.0319	6	12	18	24	30

(i) $4.55 \, \mathrm{m}$ (ii) $8.55 \, \mathrm{m}$ (iii) $6.55 \, \mathrm{m}$ (iv) $5.55 \, \mathrm{m}$ (v) $7.55 \, \mathrm{m}$

A flag is hoisted at the top of a building . From a point on the ground, the angle of elevation of the top of the flag staff is $38^{\circ}4'$ and the angle of elevation of the top of the building is $28^{\circ}12'$. If the height of the flag staff is 8 m, find the height of the building .

		From Table of Natural Tangents													
1/.	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1' 2	2' 3	3' 4'	5'
	28	0.5317	0.5340	0.5362	0.5384	0.5407	0.5430	0.5452	0.5475	0.5498	0.5520	4	8 1	1 15	19
	From Table of Natural Tangents														
	χ°	0'	6'	12'	18'	24'	30'	36'	42'	48'	54'	1' 2	21 3	3' 4'	5'
	38	0.7813	0.7841	0.7869	0.7898	0.7926	0.7954	0.7983	0.8012	0.8040	0.8069	5	9 1	4 19	23

(i) 20.37 m (ii) 17.37 m (iii) 14.37 m (iv) 12.37 m (v) 22.37 m

Assignment Key										
1) (v)	2) (iii)	3) (i)	4) (v)	5) (ii)	6) (ii)					
7) (iv)	8) (ii)	9) (iv)	10) (ii)	11) (iv)	12) (v)					
13) (ii)	14) (v)	15) (i)	16) (iii)	17) (ii)						

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